

## 234 Quiz 9

Section:

Name:

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20 minutes. The extra two points are bonus.

1. (a)(3) Mark true or false for the following(No need to explain):

- $\int_a^b \int_c^d f(x, y) dx dy = \int_c^d \int_a^b f(x, y) dy dx$
- $\int_0^1 \int_{x^2}^x f(x, y) dy dx = \int_{x^2}^x \int_0^1 f(x, y) dx dy$
- $\int_0^{100} \int_0^{100} f(x) f(y) dx dy = \left( \int_0^{100} f(x) dx \right)^2$

(b)(4) Let  $D = \{(x, y) : 0 \leq y \leq 1, y^2 \leq x \leq 1\}$ . Compute the volume under the graph of the function  $f(x, y) = y \sin(x^2)$  and above  $D$ .

2. (5) Set up the integral in polar coordinates without solving:

The volume under  $f(x, y) = x^2$  and above the region  $D = \{(x, y) : x^2 + y^2 \geq 4, x^2 + (y - 2)^2 \leq 4\}$