

234 Quiz 3

Section:

Name:

18 minutes. The extra $6 + 6 - 10 = 2$ points are for bonus.

1. (6) Let $\vec{x}(t) = \begin{pmatrix} t^2 \\ t \end{pmatrix}$. Compute the curvature κ and the unit normal vector \vec{N} . (Hint: you may want to use $\|\lambda\vec{a}\| = |\lambda|\|\vec{a}\|$)
(To check: the curvature vector you may get is $\vec{\kappa} = \frac{2}{(1+4t^2)^2} \begin{pmatrix} 1 \\ -2t \end{pmatrix}$)
2. (6) Let $\vec{x}(t) = \begin{pmatrix} t^2 \cos t \\ t^2 \sin t \\ t^2 \end{pmatrix}$ where $t \geq 0$. Compute the acceleration at $t = 0$ and the arclength of the portion from $t = 0$ to $t = 1$.