EXAM 2

Math 212, 2017-2018 Spring, Clark Bray.

You have 50 minutes.

No notes, no books, no calculators.

YOU MUST SHOW ALL WORK AND EXPLAIN ALL REASONING TO RECEIVE CREDIT. CLARITY WILL BE CONSIDERED IN GRADING.

All answers must be simplified. All of the policies and guidelines on the class webpages are in effect on this exam.

Good luck!

Name _______

"I have adhered to the Duke Community Standard in completing this examination."

1. _______

Signature: ______

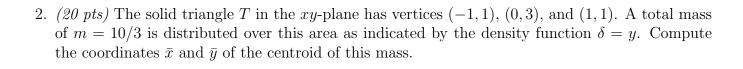
3. ______

4. ______

Total Score ______ (/100 points)

- 1. (20 pts) Let f be a function of the rectangular coordinates $x, y, and z, and let \rho, \phi, and \theta$ be the usual spherical coordinates.
 - (a) Find an expression for $\frac{\partial f}{\partial \rho}$ in terms of the rectangular partials of f and the spherical coordinates.

(b) Find an expression for $\frac{\partial^2 f}{\partial \rho^2}$ in terms of the rectangular partials of f and the spherical coordinates.



- 3. (20 pts) The solid R is bounded by the surfaces with equations $x-2y^2-2z^2+2=0$ and $x+y^2+z^2=1$. Mass is distributed in this solid with density given by $\delta(x,y,z)=e^{x-y}$.
 - Set up as an iterated triple integral the moment of inertia of this solid around the y-axis. (You do NOT have to compute the integral.)

4. (20 pts) The ellipses E_1 and E_2 in the xy-plane have equations below.

$$E_1: \left(\frac{x}{2}\right)^2 + \left(\frac{y}{1}\right)^2 = 1$$
 and $E_2: \left(\frac{x}{4}\right)^2 + \left(\frac{y}{2}\right)^2 = 1$

The region between these two ellipses is M. Compute $\iint_M x^2 dx dy$. (Hint: Use a change of variables, followed by another technique.)

5. (20 pts) The sphere S_1 is the unit sphere centered at the origin, and the sphere S_2 is the unit sphere centered at (1,0,0). The solid D consists of the points that are outside of S_1 and inside of S_2 .

Set up $\iiint_D x \, dV$ as an iterated triple integral in spherical coordinates. (You do NOT have to compute the integral.)