EXAM 2

Math 212, 2017-2018 Fall, Clark Bray.

You have 50 minutes.

No notes, no books, no calculators.

YOU MUST SHOW ALL WORK AND EXPLAIN ALL REASONING TO RECEIVE CREDIT. CLARITY WILL BE CONSIDERED IN GRADING.

All answers must be simplified. All of the policies and guidelines on the class webpages are in effect on this exam.

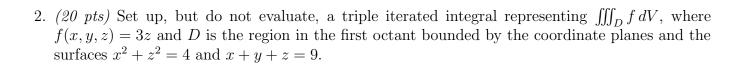
Good luck!

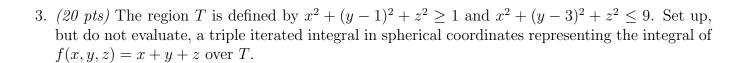
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	Total Score	(/100 points)

1.	(20 pts) The region R in \mathbb{R}^2 is bounded by the curves $x = y^2 + y + 5$ and $x = -y^2 + y + 7$. The	16
	distribution of mass on R has density $\delta(x,y) = y^2$.	

(a) Compute the total mass on R.

(b) Set up, but do not evaluate, a double iterated integral representing the moment of inertia of R around the line x=10.





4. (20 pts)

(a) The domain C in the first quadrant of \mathbb{R}^2 is bounded by the curves $xy^2 = 1$, $xy^2 = 2$, $yx^2 = 1$, and $yx^2 = 2$. Use a change of variables to set up (but not evaluate) the integral of $f(x,y) = x^5y^5\sin(xy^2 - yx^2)$ as an iterated integral.

(b) Find the value of the integral from part (a) without using change of variables.

5. (20 pts) The gradient vector for the function $f: \mathbb{R}^2 \to \mathbb{R}^1$ is

$$\nabla f(x,y) = (y^3 - 2xy, 3xy^2 - x^2)$$

The surface S is the part of the graph of f over the rectangle $[1,2] \times [3,4]$, and mass is distributed over S with density $\delta(x,y,z) = x^2y^2$.

Set up, but do not evaluate, a double iterated integral representing the mass on S.