EXAM 2

Math 212, 2013-2014 Spring, Clark Bray.

You have 50 minutes.

No notes, no books, no calculators.

YOU MUST SHOW ALL WORK AND EXPLAIN ALL REASONING TO RECEIVE CREDIT. CLARITY WILL BE CONSIDERED IN GRADING.

All answers must be simplified. All of the policies and guidelines on the class webpages are in effect on this exam.

Good luck!

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7	Total Score	(/100 points)

1. (10 pts) Find the equation of the tangent plane to the surface $x^2 + y^4 - z^2 = 8$ at the point (1,2,3).

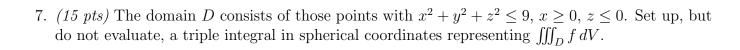
2. (10 pts) Suppose that z is a differentiable function of x and y, and that x and y are differentiable functions of s and t. For certain values of s and t, we know that $\frac{\partial z}{\partial x} = 3$, $\frac{\partial z}{\partial y} = 2$, $\frac{\partial z}{\partial s} = 5$, and $\frac{\partial y}{\partial s} = 4$. Compute $\frac{\partial x}{\partial s}$.

3. (10 pts) Suppose $3xy + y^2z - 2z^2 + 9 = 0$. At the point (2, 1, 3), what is $\frac{\partial y}{\partial z}$? (Be sure to explain all necessary steps!)

4. (10 pts) The function $f: \mathbb{R}^2 \to \mathbb{R}$ is given by $f(x,y) = x^3y^2 - 3xy$. The point $\vec{x} = (x,y)$ is at (1,2), and moving with speed 3 in the direction of fastest increase of f. Compute $\frac{df}{dt}$.

5. (15 pts) A population of bacteria is spread over the part of the unit disk where either x or y (or both) is greater than or equal to zero. The population density (in millions per unit area) is given by $\delta(x,y) = x^2$. Compute the total population of bacteria.

6. (15 pts) Use change of variables to compute the area of the region in the xy-plane described by $2 \le 3x + y \le 5$ and $1 \le x + 6y \le 4$.



8. (15 pts) The line L is parallel to the z-axis and passes through (3,4,0). The solid tetrahedron T is bounded by the coordinate planes and 2x+y+3z=6, with density given by $\delta(x,y,z)=1+x^2$. Set up, but do not evaluate, a triple integral in rectangular coordinates that represents the moment of inertia of T around L.