## EXAM 3

Math 103, Spring 2008-2009, Clark Bray.
You have 50 minutes.
No notes, no books, no calculators.
YOU MUST SHOW ALL WORK AND EXPLAIN ALL REASONING TO RECEIVE CREDIT. CLARITY WILL BE CONSIDERED IN GRADING.

Good luck!

Name $\qquad$
ID number $\qquad$

1. $\qquad$
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7. $\qquad$
Total Score $\qquad$ (/100 points)
8. (16 pts) Let $R$ be the region in $x y z$-space bounded by the six surfaces $x+y+z=1$, $x+y+z=3,2 x+y=0,2 x+y=1, y+4 z=2$, and $y+4 z=5$. Compute the integral

$$
\iiint_{R}(2 x+y)^{2} d x d y d z
$$

2. (14 pts) Write down and simplify, but do not evaluate, a single triple nested integral (in whatever coordinate system you can) that represents the volume of the part of the ball $x^{2}+(y-1)^{2}+z^{2} \leq 1$ that is outside of the cone $\phi=\pi / 6$ and inside the cone $\phi=\pi / 3$.
3. (14 pts) Write down and simplify, but do not evaluate, a nested integral representing the area of the part of the surface $4+x^{2}-y-z^{2}=0$ that is inside the cylinder $x^{2}+z^{2}=2$.
4. (14 pts) Let $C$ be the part of the curve $y=x^{2}$ with $0 \leq y \leq 1$, oriented to the left. Compute the line integral over this curve of the field $\vec{F}=(3 y,-2 x)$.
5. (14 pts) Let $C$ be the curve parametrized by $\vec{r}(t)=\left(t^{2}-4 t+5, \cos (2 \pi t) e^{t^{4}-t}, \sin (2 \pi t)\right)$, with $t \in[0,1]$. Compute the line integral over this curve of the field $\vec{F}=\left(2 x e^{y z}, x^{2} z e^{y z}, x^{2} y e^{y z}\right)$.
6. (14 pts) Let $C$ be the rectangle with vertices at $(0,0),(2,0),(0,3),(2,3)$, oriented clockwise. Compute the line integral over this curve of the field $\vec{F}=\left(x^{2} y+x e^{x^{3}}, x y-\sin ^{2}\left(e^{y}\right)\right)$.
7. (14 pts) Let $S$ be the part of the surface $z=\left(x^{2}+y^{2}-1\right)\left(x^{4}+y^{4}+1\right)$ that is below the plane $z=0$, oriented upward. Compute the flux through this surface of the field $\vec{F}=\left(x y^{3}+y^{2} z, x^{2} z^{2}-x^{2} y, z x^{2}-z y^{3}\right)$.
